



SMF2: Global model of the F2 layer peak height based on satellite data

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International Reference Ionosphere (IRI)

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Approach

IRI:

$$h_m F2 = \text{Approximation}(M3000, f_o F2 / f_o E, R_z)$$

SMF2:

$$h_m F2 = \text{SHA}(\varphi, \lambda) * \text{Fourier}(t) * \text{Corr}(F_{10.7A})$$

Based on a set of $149 \times 24 \times 12 = 42912$ coefficients
(for low and high activity)

Data set

2 800 000 COSMIC profiles (<http://www.cosmic.ucar.edu>)

100 000 GRACE profiles (<http://op.gfz-potsdam.de/champ/>)

300 000 CHAMP profiles (<http://op.gfz-potsdam.de/champ/>)

200 000 Interkosmos-19 profiles

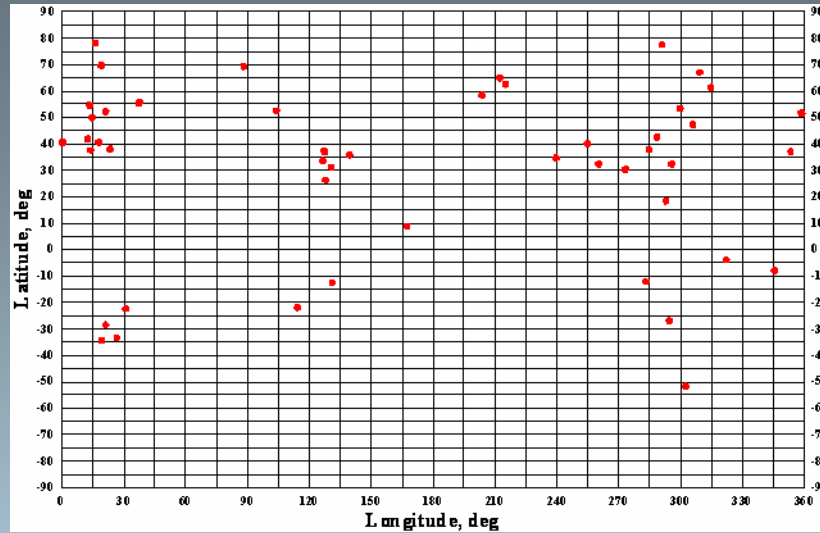
For high solar activity ~60 Digisonde stations were added
(<http://ulcar.uml.edu>)

Low solar activity ($F_{10.7} \leq 80$)

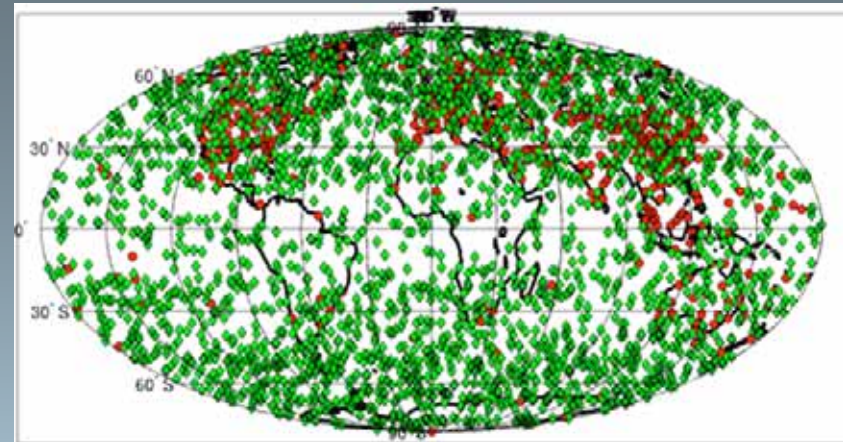
- Mainly COSMIC, also some CHAMP and GRACE data
- GPS radio occultation data
- A form of Abel transform is used to derive profiles and $h_m F2$
- Ready-for-use profiles were downloaded

Data global distribution

Digisondes



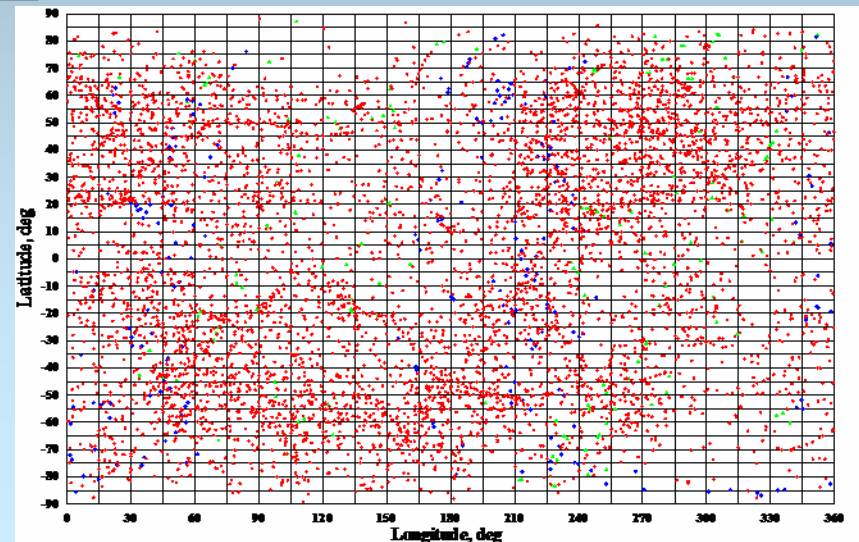
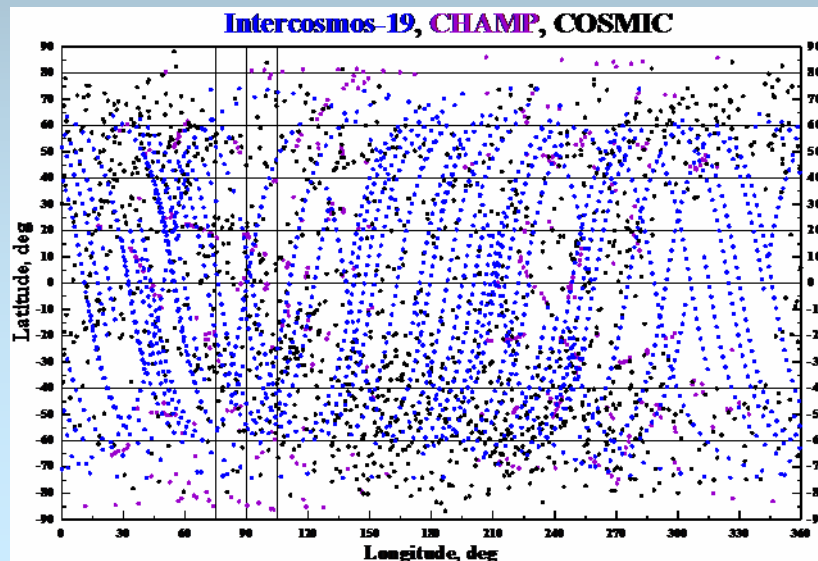
One day COSMIC observations



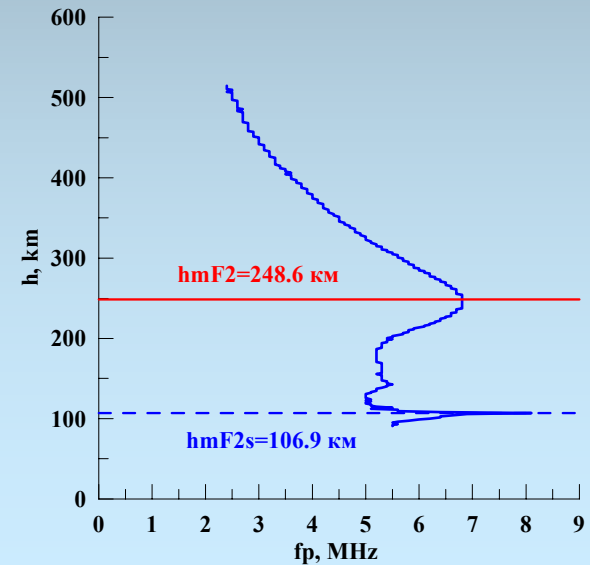
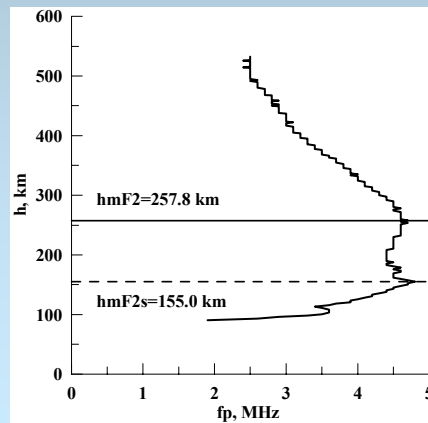
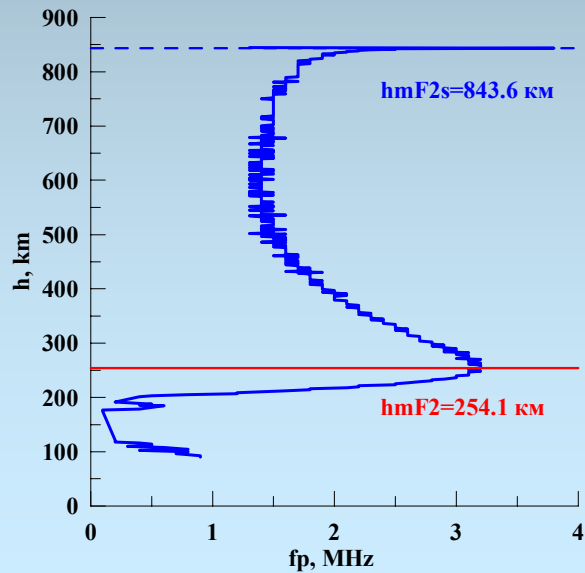
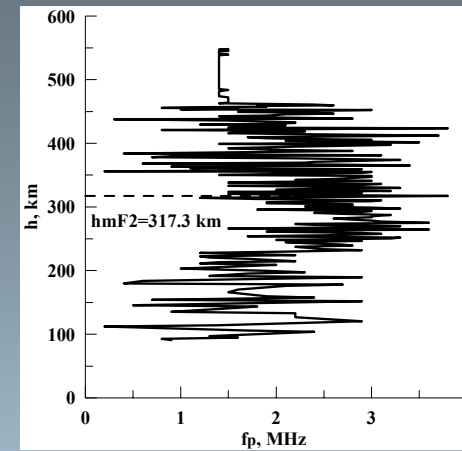
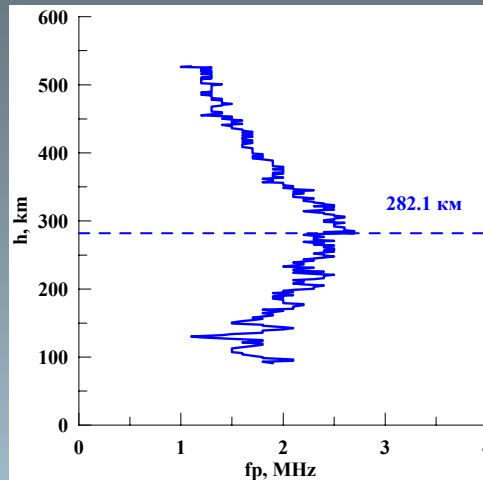
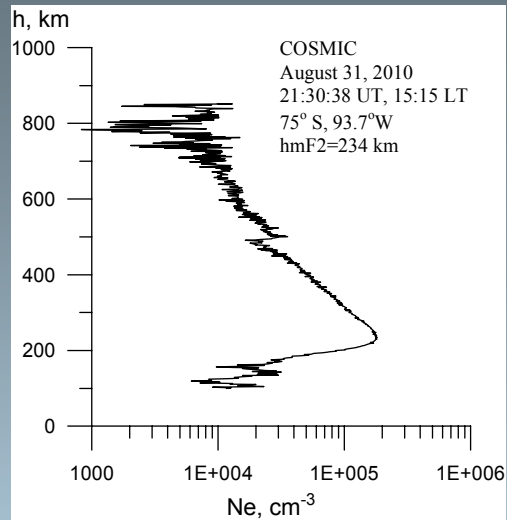
High solar activity ($F10.7A > 140$), December, 00 UT

860
bins

Low solar activity ($F10.7A < 80$), January, 00 UT
COSMIC, CHAMP, GRACE



Typical Problems with Occultation Profiles

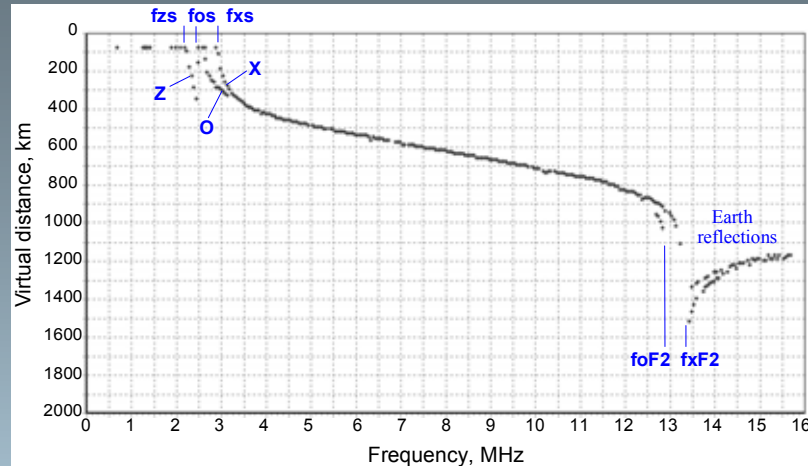


High solar activity ($F_{10.7A} > 140$)

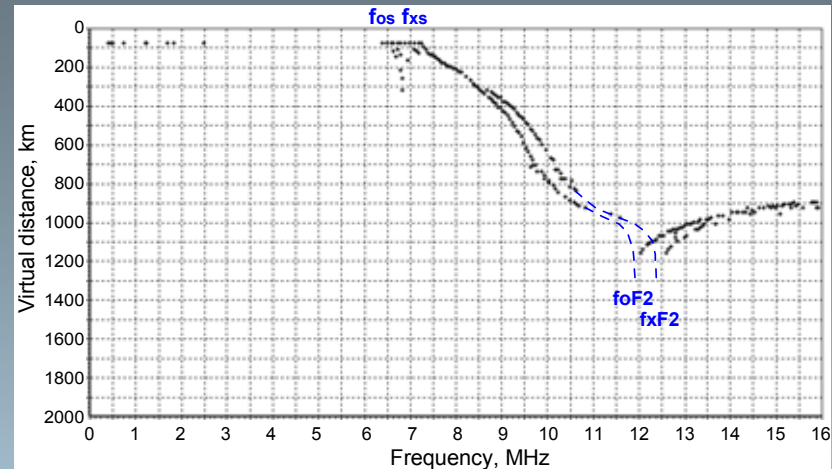
- Mainly Interkosmos-19 data (1979—1981)
- Top-side ionograms
- Close-to-uniform global coverage
- Restored from tapes and prints
- Manually scaled
- A variation of Jackson algorithm is used to derive profiles and $h_m F2$
- In addition – some CHAMP, GRACE and Digisonde data

Typical Problems with IK-19 data

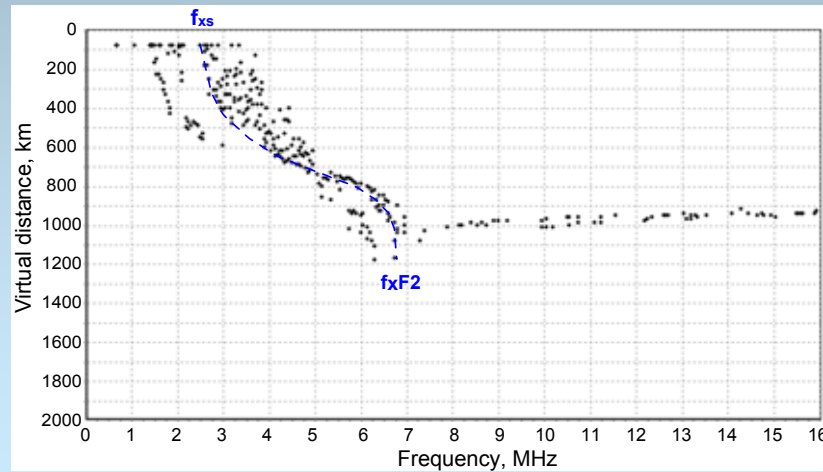
Strong radio signal attenuation near critical frequency



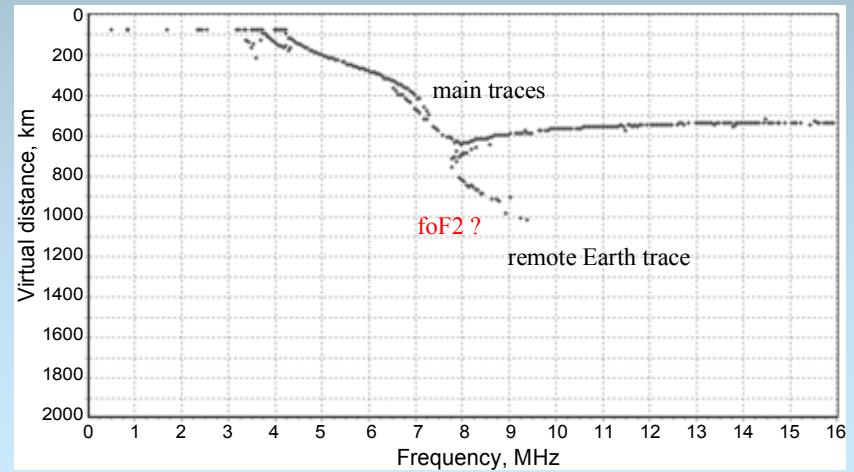
Ionogram with F3-layer



Strong F-spread



Remote reflection from ground



Model Construction

Method of the model construction

Modeling of the spatial dependencies is based on expansion of these dependencies in series by a system of orthogonal functions [Chernyshov, Vasilyeva, 1973]. The $h_m F2$ dependency on latitude φ and longitude λ in some fixed moment of time is expanded as a series:

$$F(\phi, \lambda) = \sum_{m=0}^M \sum_{n=m}^N [g_n^m \cos m\lambda + h_n^m \sin m\lambda] \cdot P_n^m(\cos \vartheta), \quad (1)$$

where $\vartheta = 90^\circ - \varphi$, g_n^m and h_n^m are expansion coefficients, and $P_n^m(\cos \vartheta)$ are associated **Legendre functions**. The coefficients in (1) are determined with the least square method. The series (1) could be presented in a shorter form:

$$F(\phi, \lambda) = \sum_{k=0}^K D_k \cdot G_k(\phi, \lambda), \quad k=0, 1, 2, \dots, K, \quad (2)$$

where D_k are complex expansion coefficients and $G_k(\phi, \lambda)$ are spherical harmonics. The number of the coefficients is determined as $K = m \cdot (2n - m + 1) + n + 1$. To determine coefficients in (2) we used Gram-Schmidt orthonormalising, as in [Chernyshov, Vasilyeva, 1973]. The approximation was considered to be optimal when the standard deviation SD was minimized for the given month and UT hour:

$$SD = \sqrt{\frac{1}{n-1} \left[\sum_{i=1}^n (h_m F2 - h_m F2_{\text{mod}})^2 - \frac{1}{n} \left(\sum_{i=1}^n (h_m F2 - h_m F2_{\text{mod}}) \right)^2 \right]}, \quad (3)$$

We chose as optimal $M = 8$ (longitudinal) и $N = 12$ (latitudinal) numbers. Thus, we need **149** coefficients for one month and UT hour.

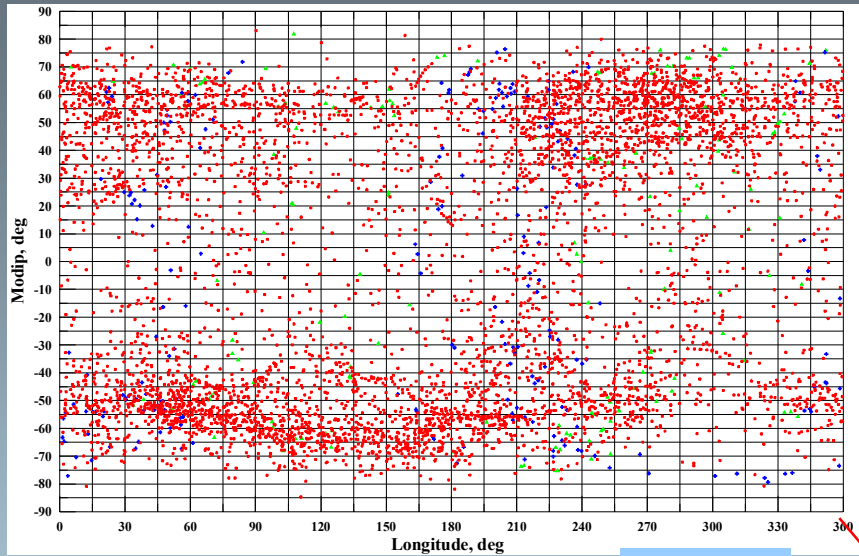
For the diurnal interpolation we have used a **Fourier decomposition** with **3** harmonics:

$$F(t) = \sum_{i=0}^3 \left[a_i \cos\left(i \frac{2\pi}{T} t\right) + b_i \sin\left(i \frac{2\pi}{T} t\right) \right], \quad (4)$$

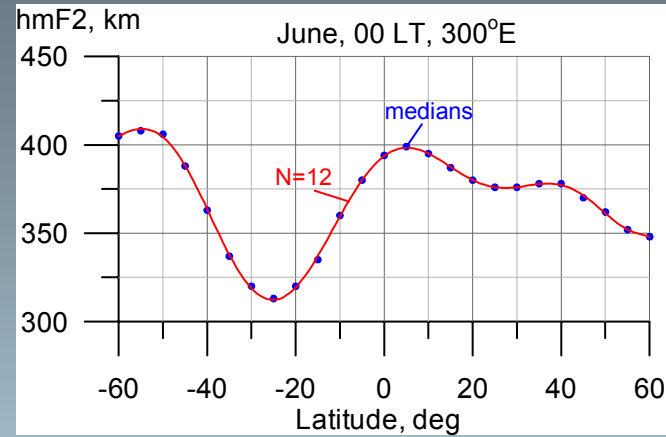
where a_i and b_i are found from $h_m F2$ diurnal dependency with period $T = 24$ hours with the help of Gram-Schmidt process.

Model construction

MODIP

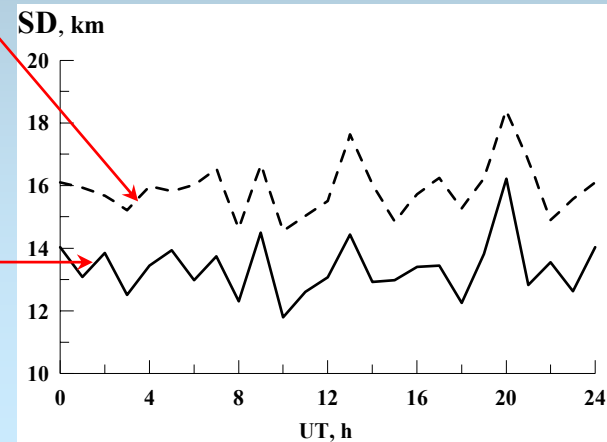
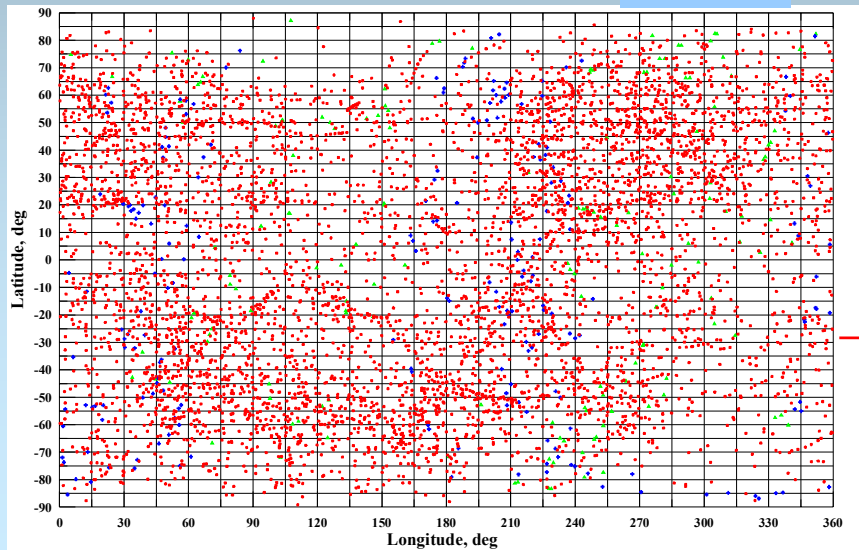


Latitudinal variations, N=12
Longitudinal variations, M=8

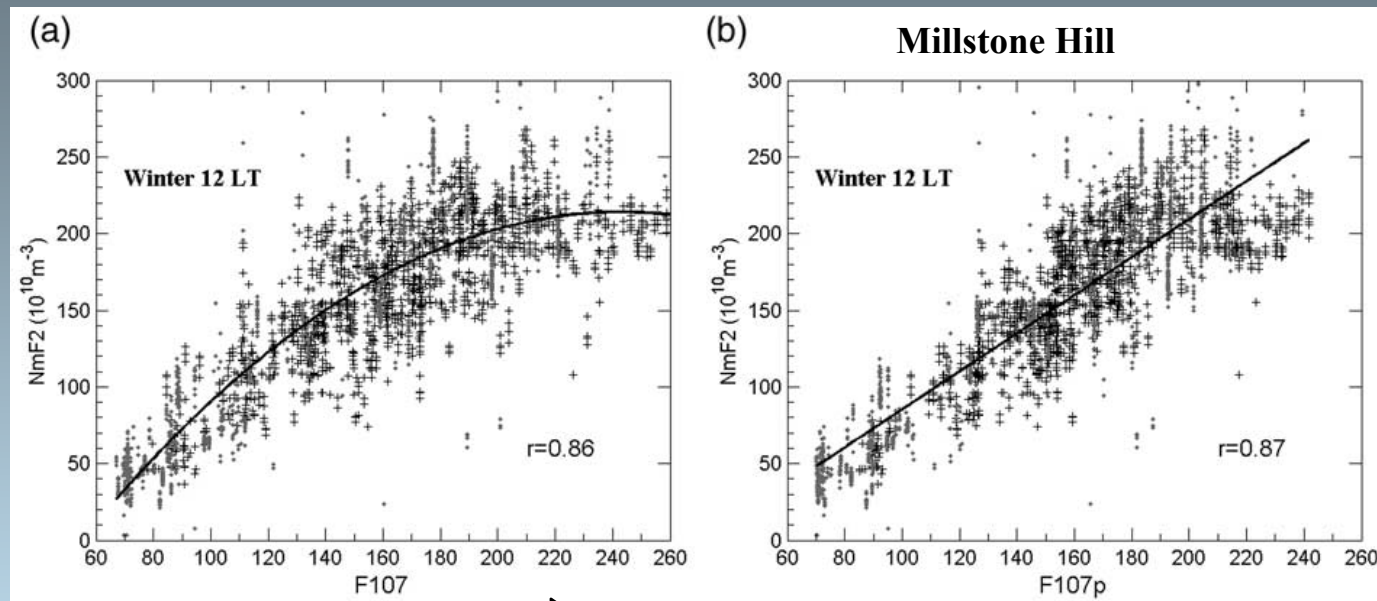


Geographic latitude

January
00 UT



$N_m F2$ and $h_m F2$ dependence on solar activity



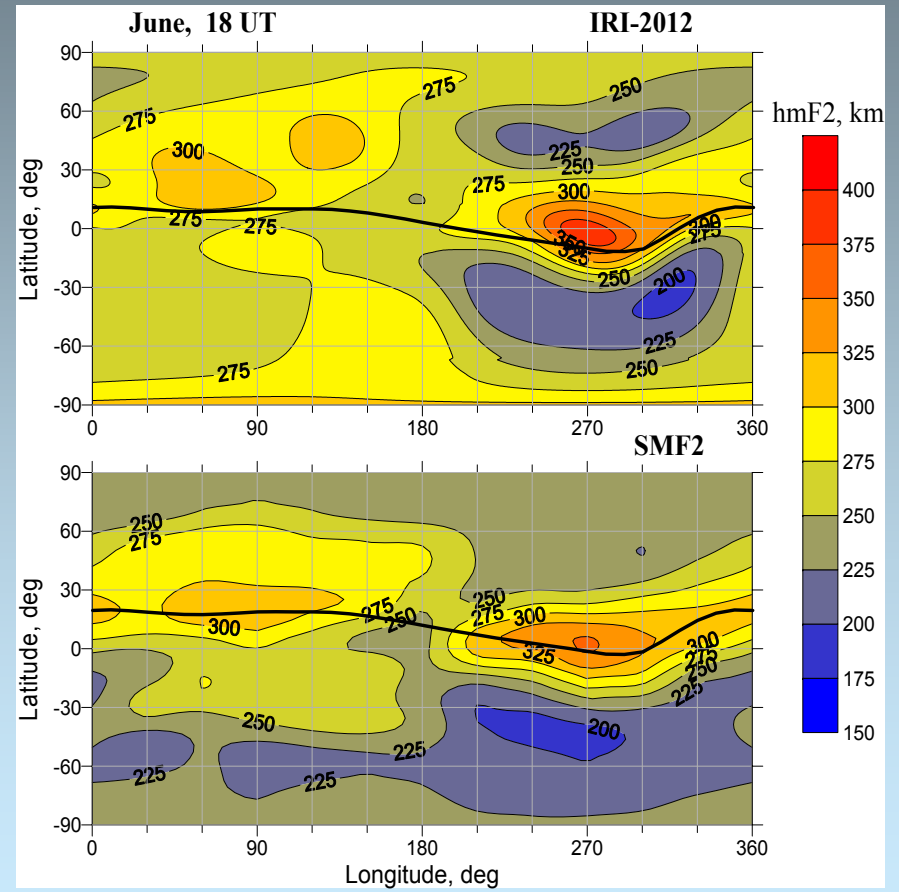
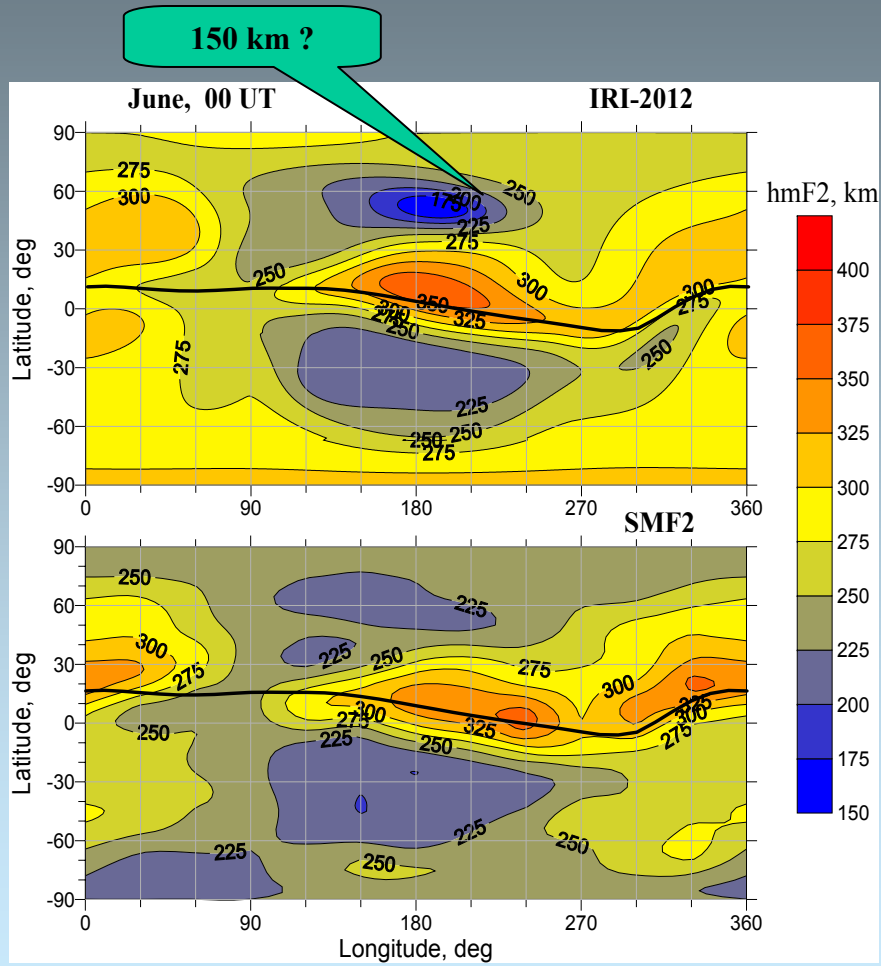
Lei et al., Radio Sci., v.40. 2005.

$F_{10.7A}$ is daily $F_{10.7}$ averaged for 3 rotations of the Sun

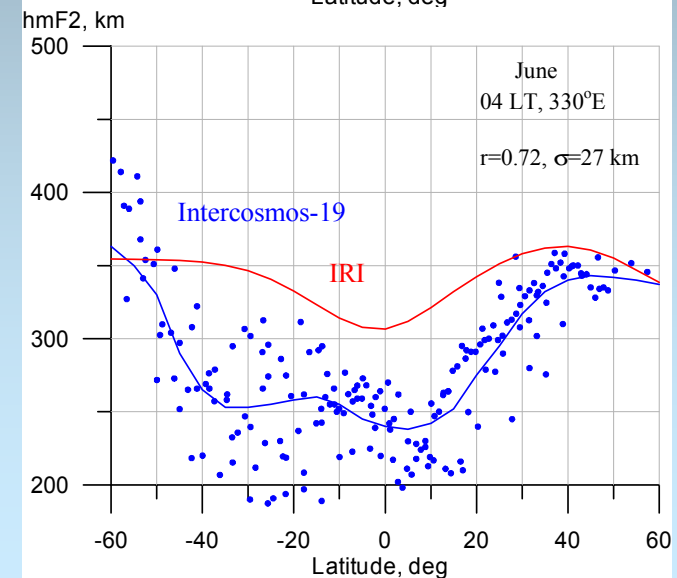
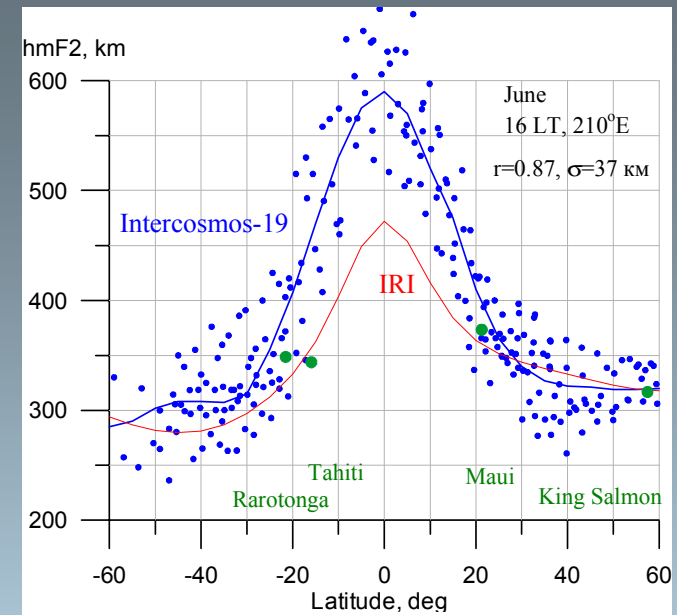
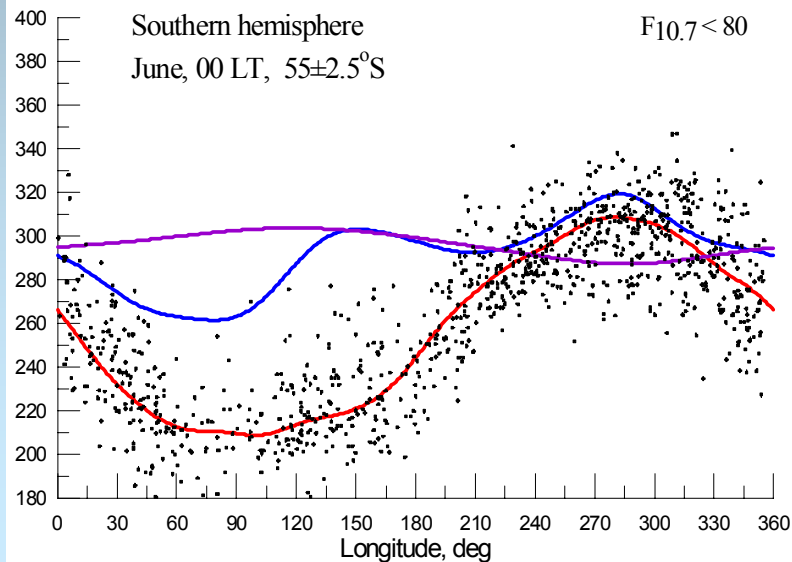
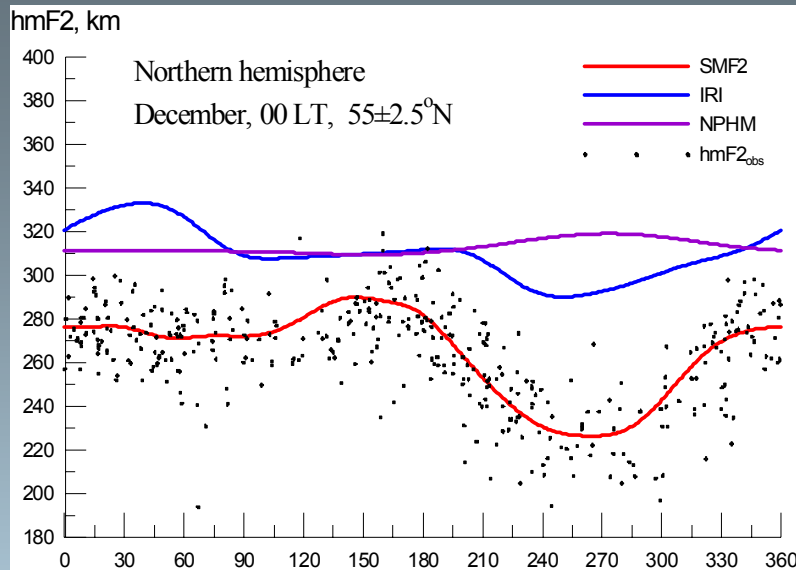
$$F_{10.7p} \text{ (proxy)} = (F_{10.7} + F_{10.7A}) / 2$$

Checking, Testing and Validation of the Model

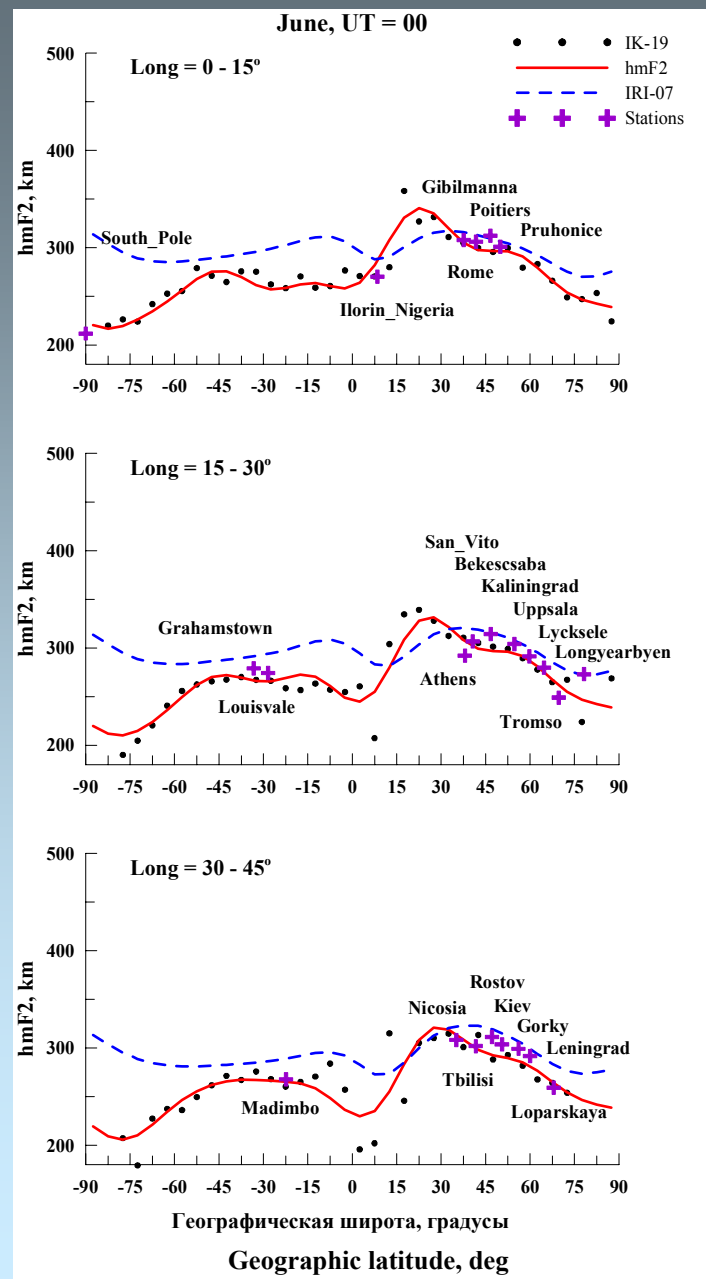
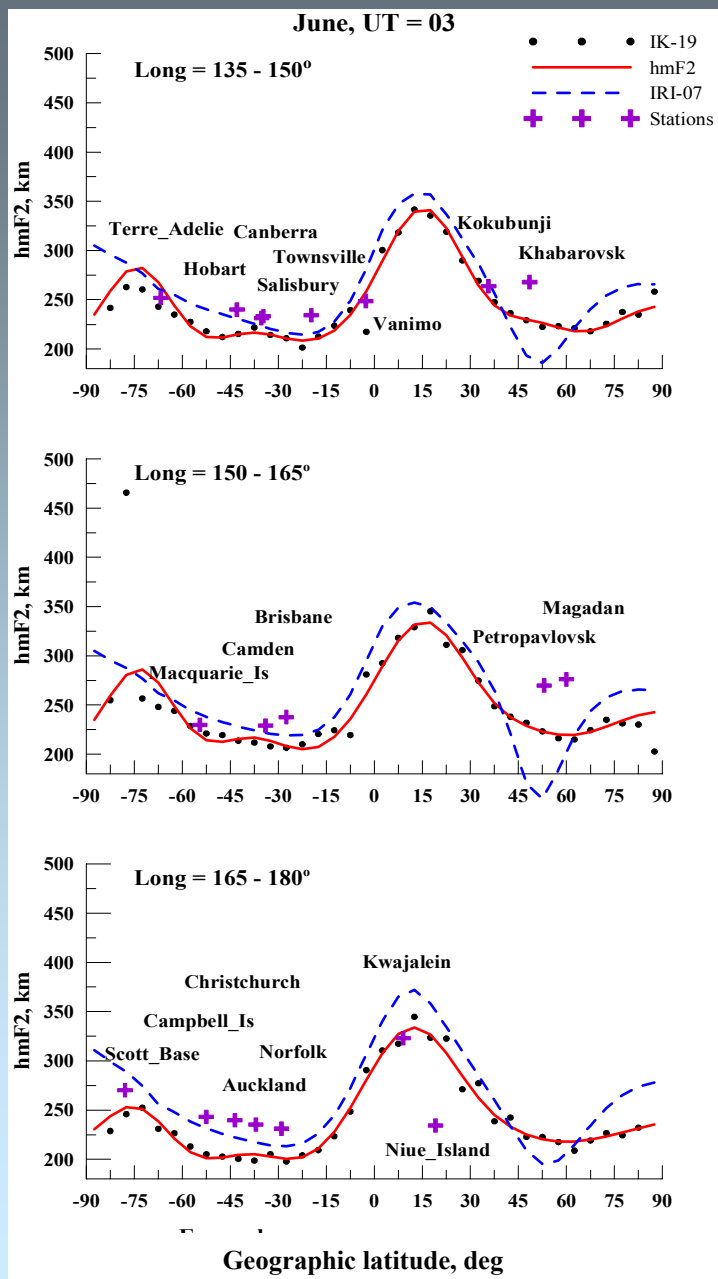
SMF2 and IRI comparison: Low solar activity



Longitudinal and Latitudinal variations



Latitudinal variations: High solar activity



SMF2-IRI Comparison

(June, High and Low Solar Activity)

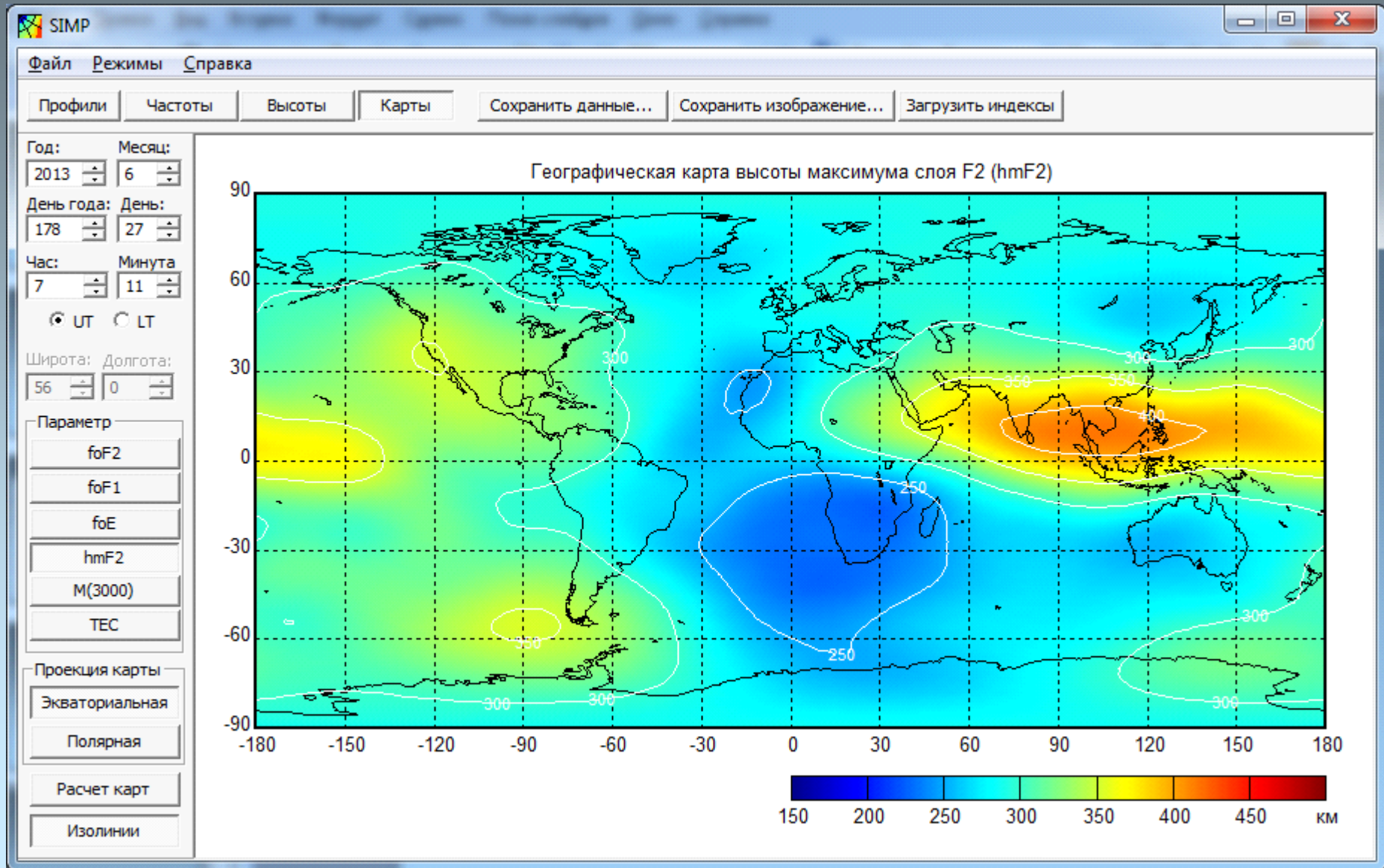
UT, h	N	SMF2			IRI-2012		
		SD, km	SCAT, km	MRD %	SD, km	SCAT, km	MRD %
00	822	11.83	11.82	3	23.96	32.76	11
01	827	11.34	11.33	3	22.97	30.25	10
02	830	10.78	10.78	3	23.04	29.49	10
03	831	13.26	13.25	3	23.14	28.90	9
04	825	11.74	11.73	3	22.23	27.90	9
05	829	12.68	12.67	3	21.59	26.84	8
06	830	12.00	11.99	3	22.80	29.00	9
07	832	11.38	11.38	3	22.74	29.84	10
08	832	11.42	11.41	3	23.44	31.39	10
09	839	10.41	10.40	3	23.53	32.12	11
10	829	11.61	11.61	3	25.64	34.55	12
11	833	11.50	11.49	3	24.75	34.67	12
12	813	12.71	12.71	3	25.51	34.59	12
13	829	11.76	11.76	3	23.96	33.19	11
14	830	9.87	9.87	3	23.99	33.20	11
15	826	10.41	10.40	3	25.53	33.00	11
16	823	10.40	10.39	3	25.46	34.11	11
17	821	12.08	12.08	3	25.60	33.72	11

UT h	N	SMF2			IRI-2012		
		SD, km	SCAT, km	MRD %	SD, km	SCAT, km	MRD %
04	164	21.91	21.84	5	31.34	32.54	7
05	153	22.94	22.89	5	37.53	41.14	9
06	164	19.78	19.74	4	33.35	33.74	8
07	156	21.89	21.85	5	35.50	37.46	8
08	126	17.98	18.00	4	31.72	33.45	7
09	119	18.42	18.35	4	37.18	38.18	8
10	101	19.89	19.81	4	40.03	44.58	8
11	111	16.98	16.97	4	49.25	50.90	10
12	122	20.09	20.03	4	49.90	56.95	9
13	118	19.92	19.90	4	39.13	39.83	9
14	124	17.84	17.77	4	35.83	35.72	9
15	111	19.05	19.04	5	39.44	39.39	9
16	120	25.72	25.75	7	44.87	44.69	12
17	93	21.40	21.34	5	36.44	36.27	8
18	99	25.85	25.91	5	43.26	44.55	9
19	89	21.59	21.56	5	44.00	43.90	10
20	111	17.63	17.59	4	39.08	38.91	11
21	174	19.71	19.66	5	44.42	44.30	11

Technical implementation

- ~400 lines of FORTRAN code
- Compiled for Windows and Linux OS
- Open and free for distribution (in near future)
- Command-line interface
- C++ Windows graphical interface
- Web interface (<http://space-weather.ru>)

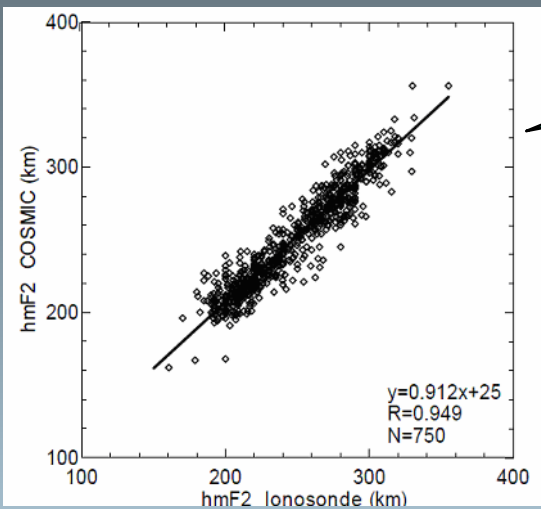
Windows Graphical Interface



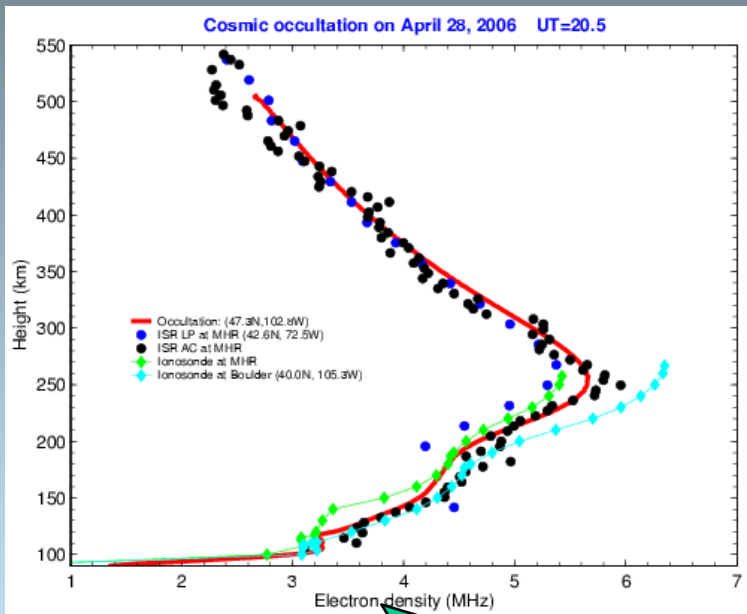
Conclusions

- A global median $h_m F2$ model based on the vast satellite database is created, with relative deviations (*MRD*) for all months 2–3 times less than in IRI
- The approach looks promising
- More data necessary for high solar activity
- A problem of correct validation is noted

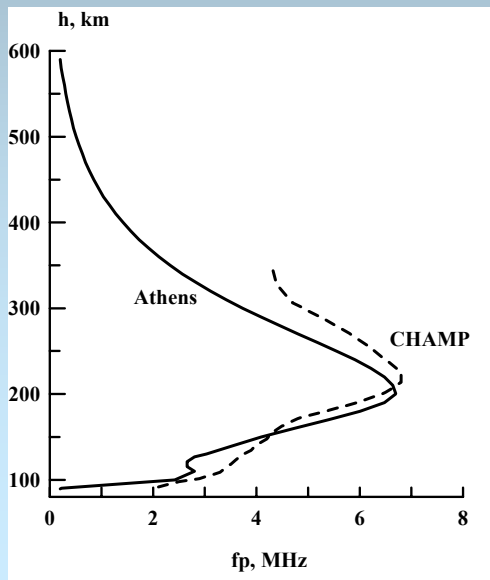
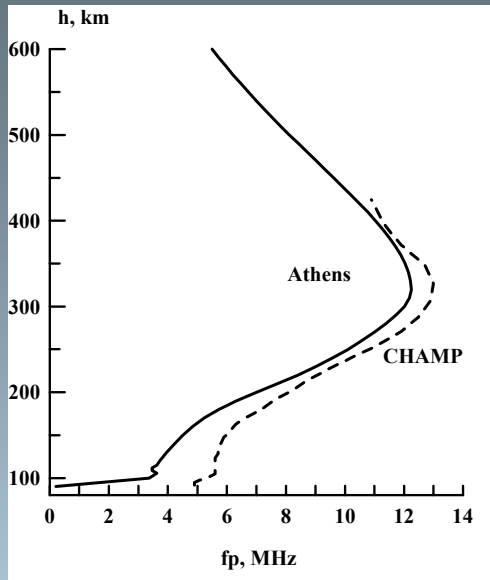
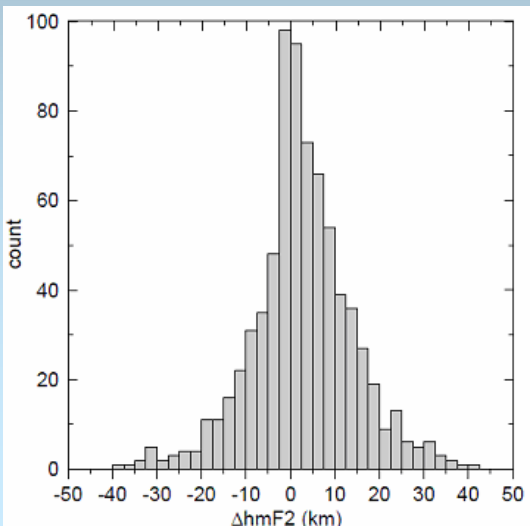
Comparison between COSMIC and ionosondes



Krankowski et al., J. Geod., 2011.



Cheng et al., 4th ASC, 2008, Taipei, Taiwan



Latitudinal variations:

Pacific

High solar activity

Low solar activity

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