

RELATIONSHIPS BETWEEN GEOMETRIC PARAMETERS IN CONICAL ROTARY GRADERS

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Key words: rotary grader, conical working surface, geometry.

Abstract

The objective of this study was to determine the formula for the radius describing the position of a point located on the conical working surface relative to the vertical axis of revolution in circular motion. Diagrams of conical working surface were presented, and a formula for the above radius was determined. The relationship was verified for randomly selected points on the conical surface, using a 3D model.

ZALEŻNOŚCI MIĘDZY WIELKOŚCIAMI GEOMETRYCZNYMI W STOŻKOWYCH TRYJERACH OBIEGOWYCH

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Słowa kluczowe: tryjer obiegowy, stożkowa powierzchnia robocza, geometria.

Abstrakt

Praca dotyczy wyznaczenia zależności na promień położenia punktu znajdującego się na stożkowej powierzchni roboczej względem pionowej osi obrotu w ruchu obiegowym. Przedstawiono schematy stożkowej powierzchni roboczej i wyprowadzono ściśle zależność na wspomniany promień. Zweryfikowano uzyskaną zależność na modelu 3D dla dowolnie wybranych punktów leżących na powierzchni stożkowej.

\vec{w} – relative velocity,
 \vec{a}_u – acceleration of transport,
 \vec{a}_w – relative acceleration,
 \vec{a}_c – Coriolis acceleration.

At given operating parameters ($\omega_2 = \text{const.}$), the velocity and acceleration of transport (Fig. 1) will take on the following form:

$$\vec{u} = \vec{\omega}_2 \times \vec{R}_\beta, \quad \vec{a}_u = \vec{a}_u^n = \vec{\omega}_2 \times (\vec{\omega}_2 \times \vec{R}_\beta) \quad (2)$$

where:

\vec{a}_u^n – normal acceleration of transport (centripetal).

If $\vec{\omega}_2 \perp \vec{R}_\beta$, the velocity and acceleration of transport can be calculated based on the following scalar dependencies:

$$u = \omega_2 \cdot R_\beta, \quad a_u = (\omega_2)^2 \cdot R_\beta \quad (3)$$

In general, R_β should be a function of the grader's geometric parameters which define the position of point B on the conical surface. As shown in Figure 1, radius R_β should be determined by:

- radius R of cone's circular motion (distance between the cone's own axis of revolution ξ and axis z of circular motion),
- radius r_o of cone's intersection with plane $\eta\zeta$ w in mid-length,
- angle α_p at which a seed slides down the surface of the working element,
- angle φ between the cone's element and the cone's own axis of revolution ξ ,
- angle β between the radius of cone's circular motion and radius R_β .

In JADWISIEŃCZAK (2007), R_β has been incorrectly determined, therefore, the objective of this study was to determine the correct relationship describing radius R_β .

Figure 1 presents radii R_β and R_{β^*} and angles β and β^* describing the position of points B and B^* on the opposite sides of plane $\eta\zeta$ (intersecting the cone in mid-length). As demonstrated later, the relationships applicable to R_β and R_{β^*} will differ only in sign (+, -), therefore index (*) will not be used in successive parts of the study.

Geometric relationship

The input values were R , r_o , α_p , φ , β . The searched function will support the determination of the distance between point B and axis z , i.e. $R_\beta = f(R, r_o, \alpha_p, \varphi, \beta)$.

As demonstrated by Figure 2, distance R between axis z of cylinder's circular motion and the cylinder's own axis of revolution ξ is equal to:

$$R = KO_2 + AB \quad (8)$$

Triangles BKO_2 and ABO produce the following equations:

$$KO_2 = R_\beta \cos \beta, \quad AB = r_\beta \sin \alpha_p \quad (9)$$

therefore, when equations (9) are substituted in formula (8), the result is:

$$R = R_\beta \cos \beta + r_\beta \sin \alpha_p \quad (10)$$

Dependence (7) is substituted in equation (10) to produce:

$$R = R_\beta \cos \beta + r_\beta \sin \alpha_p - R_\beta \sin \beta \operatorname{tg} \varphi \sin \alpha_p \quad (11)$$

After simple transformation, the result is a relationship between radius R_β and point B situated behind intersecting plane $\eta\zeta$:

$$R_\beta = \frac{R - r_o \sin \alpha_p}{\cos \beta - \sin \beta \operatorname{tg} \varphi \sin \alpha_p} \quad (12)$$

Figure 3 presents geometric parameters required for the determination of radius R_β for point B situated behind intersecting plane $\eta\zeta$. For this part of the cone, the following dependence is derived from triangle EBD :

$$\operatorname{tg} \varphi = \frac{r_\beta - r_o}{s} \quad (13)$$

therefore, radius r_β describing the location of point B relative to the cylinder's own axis of revolution ξ can be presented in the following form:

$$r_\beta = r_o + s \cdot \operatorname{tg} \varphi \quad (14)$$

A comparison of Figure 2 and Figure 3 indicates that equation (6) has an identical form in both cases. When equation (6) is substituted in dependence (14), the result is:

$$r_\beta = r_o + R_\beta \sin \beta \operatorname{tg} \varphi \quad (15)$$

Verification of relationship

A 3D model of the part of the cone in front of intersecting plane $\eta\zeta$ has been developed in the AutoCAD application (Fig. 2). The following model data were input: $R=1000$ mm, $r_o=200$ mm, height of beveled cone = 300 mm, radius of the smaller base = 100 mm (Fig. 4). Points B_1 and B_2 were mapped on the cone's lateral surface at two angles of α_p . Angles φ and β and the corresponding radii $R\beta$ were measured (Fig. 4), and the resulting values were presented in Table 1. The length of radii $R\beta$ determined based on dependence 12 is shown in the last column of Table 1.

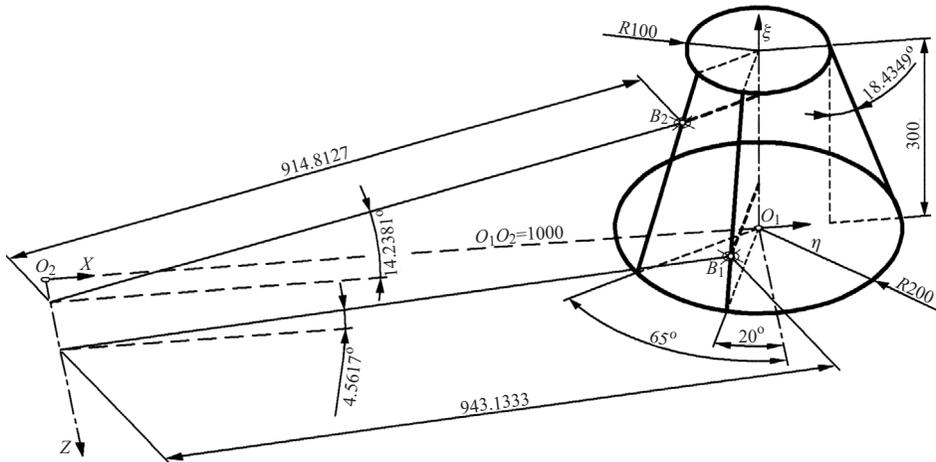


Fig. 4. A 3D model, radius and angle measurements

Table 1

Geometric parameters for point B

Point	Angle [°]			Radius R_β [mm]	
	α_p	φ	β	measured	based on (12)
B_1	20	18.4349	4.5611	943.1333	943.13326
B_2	65		14.2381	914.8127	914.81252

Conclusions

The relationship describing the distance between point B and axis z of cone's circular motion was determined in this study. In section 3, the formula (12) describing radius R_β was verified. The convergence between the measured

values of R_β and the values of R_β derived from equation (12) is determined solely by the rounding-off of the values of trigonometric functions of angles α_p , φ and β . Therefore, it can be concluded that equations (12) and (17) have been formulated correctly.

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